

Section 1.6: Inequalities

Key Topics: inequalities, identity, methods of solving inequalities

Nonnegative Identity

$$x^2 \geq 0$$

for any real number x .

The following operations produce _____ inequalities:

1. Simplifying one or both _____ of an inequality by _____ like terms and _____ parentheses
2. Adding or subtracting the _____ expression _____ sides of the inequality

If C represents a real number, then the following inequalities are all equivalent.

Sign of C	Inequality	Sense	Example
	$A < B$	$<$	$3x < 12$
C _____	$A \cdot C < B \cdot C$	_____	$\frac{1}{3}(3x) < \frac{1}{3}(12)$
C _____	$\frac{A}{C} < \frac{B}{C}$	_____	$\frac{3x}{3} < \frac{12}{3}$
C _____	$A \cdot C > B \cdot C$	_____	$-\frac{1}{3}(3x) > -\frac{1}{3}(12)$
C _____	$\frac{A}{C} > \frac{B}{C}$	_____	$\frac{3x}{-3} > \frac{12}{-3}$

_____ results apply when $<$ is replaced throughout with _____ of the symbols \leq , $>$, or \geq .

Using the Test-Point Method to Solve an Inequality

Step 1 _____

Step 2 _____

Step 3 _____

Step 4 _____

Step 5 _____

Step 6 _____

Solve the inequality.

$$x^3 - 2x^2 - 15x > 0$$

Solve the inequality.

$$\frac{x^2 - 3x - 18}{x^2 - 4} \leq 0$$

Section 1.7: Equations and Inequalities Including Absolute Value

Key Topics: absolute value equations, absolute value inequalities

Solutions of $|u| = a, a \geq 0$

If $a \geq 0$ and u is an algebraic expression, then

$|u| = \underline{\hspace{1cm}}$ is equivalent to $u = a$ or $u = -a$.

$|u| = \underline{\hspace{1cm}}$ has $\underline{\hspace{1cm}}$ solution when $\underline{\hspace{1cm}}$.

Rules for Solving Absolute Value Inequalities

If $a > 0$ and u is an algebraic expression, then

1. $|u| < a$ is equivalent to $\underline{\hspace{1cm}}$, or u in $\underline{\hspace{1cm}}$.
2. $|u| \leq a$ is equivalent to $\underline{\hspace{1cm}}$, or u in $\underline{\hspace{1cm}}$.
3. $|u| > a$ is equivalent to $\underline{\hspace{1cm}}$, or u in $\underline{\hspace{1cm}}$.
4. $|u| \geq a$ is equivalent to $\underline{\hspace{1cm}}$, or u in $\underline{\hspace{1cm}}$.

Work the Practice Problems in this section.