

Sections 8.2,8.3: Ellipses and Hyperbolas

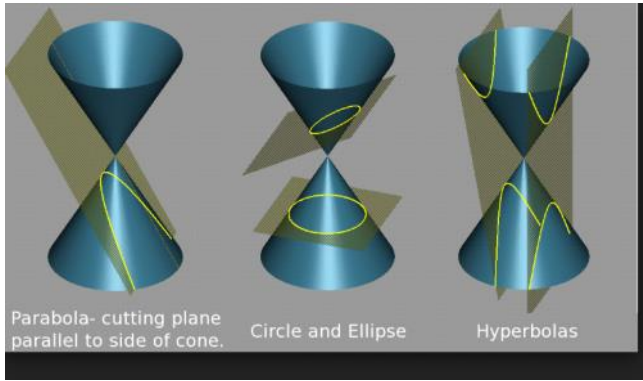
Friday, April 04, 2014
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Homework is from the text:

8.2: 9-33 e.o.o.

8.3: 9- 29 e.o.o.

DON'T WORRY ABOUT FINDING FOCI OR EQUATIONS OF ASYMPTOTES FOR HYPERBOLAS



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Parabola

Standard Equations

$$(x-h)^2 = 4p(y-k)$$

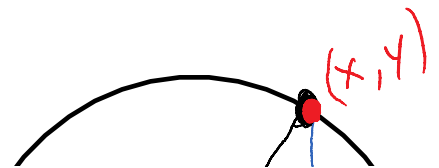
$\begin{matrix} \curvearrowright p > 0 \\ \curvearrowleft p < 0 \end{matrix}$
 $v(h, k)$

or

$$(y-k)^2 = 4p(x-h)$$

$\begin{matrix} \curvearrowright p > 0 \\ \curvearrowleft p < 0 \end{matrix}$

The Standard Equation of a circle



$$(x-h)^2 + (y-k)^2 = r^2$$

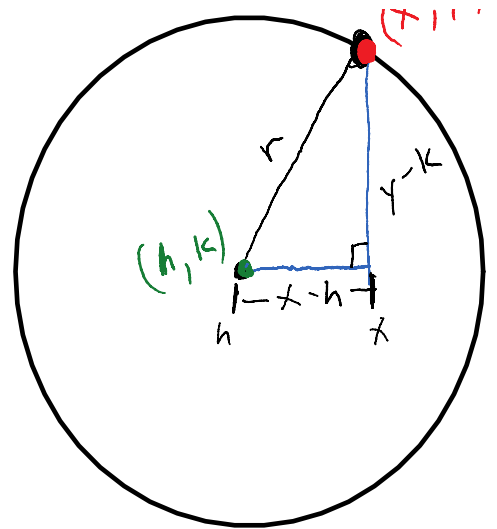
↑ standard eqn. of a circle with center (h, k) radius = r

dividing by r^2

$$\frac{(x-h)^2}{r^2} + \frac{(y-k)^2}{r^2} = 1$$

changing would stretch or compress the circle vertically

changing would stretch or compress the circle horizontally

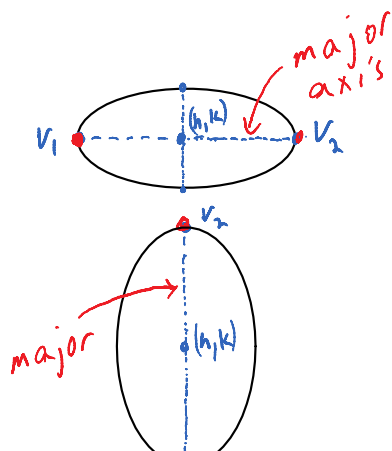


Ellipse

$$\frac{(x-h)^2}{a^2} + \frac{(y-k)^2}{b^2} = 1$$

$$\frac{(x-h)^2}{b^2} + \frac{(y-k)^2}{a^2} = 1$$

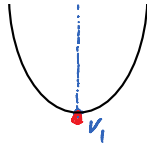
Std. eqns.
of ellipse



$$a > b$$

Std. eqns.

$$C(h, k)$$

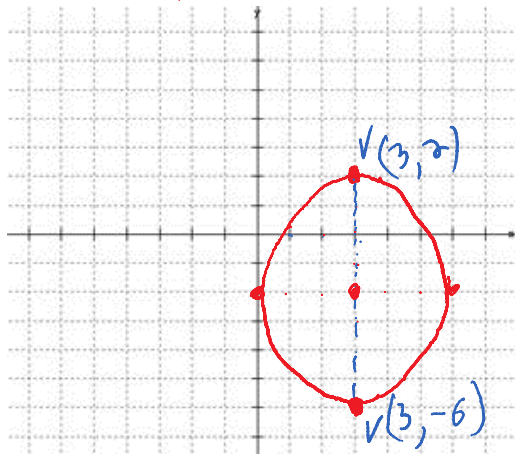


(ex) Graph $\frac{(x-3)^2}{9} + \frac{(y+2)^2}{16} = 1$

horizontal
↓
3

vertical
↓
4

$$C(3, -2)$$

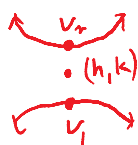


Hyperbolas

$$\frac{(x-h)^2}{a^2} - \frac{(y-k)^2}{b^2} = 1$$

$$\frac{(y-k)^2}{a^2} - \frac{(x-h)^2}{b^2} = 1$$

Std. Eqns.



(ex) Graph $\frac{(x+3)^2}{9} - \frac{(y-2)^2}{16} = 1$

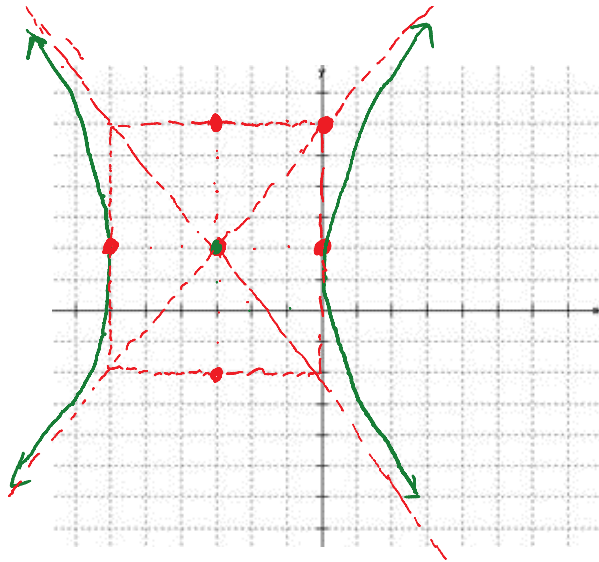
horizontal
↓
a=3

vertical
↓
b=4

$$C(-3, 2)$$



$C(-3, 2)$



Why asymptotes?

Let $C(0,0)$ be center.

$$\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$$

$$\frac{y^2}{b^2} = b^2 \left(\frac{x^2}{a^2} - 1 \right)$$

$$\sqrt{y^2} = \pm \sqrt{\frac{b^2}{a^2} x^2 - b^2}$$

$$y = \pm \sqrt{\frac{b^2}{a^2} x^2 - b^2}$$

$$y \approx \pm \sqrt{\frac{b^2}{a^2} x^2}$$

when $|x|$ gets "big"

$$y \approx \pm \frac{b}{a} x$$

← eqns. of asymptotes if center is $(0,0)$ and positive

$$y^2 \pm \frac{b}{a}x$$

← eqns. of $xy=0$
center is $(0,0)$ and y -
term involves x .

(ex) Find the center ^(or vertex) and identify the conic:

$$a) \quad \underbrace{4x^2 + 16x}_{\text{group}} + \underbrace{y^2 - 6y}_{\text{group}} = -21$$

$$\frac{(x-h)^2}{a^2} + \frac{(y-k)^2}{b^2} = 1$$

$$4(x^2 + 4x + 2^2) + y^2 - 6y + 9 = -21 + 16 + 9$$

$$\frac{4(x+2)^2}{4} + \frac{(y-3)^2}{4} = \frac{4}{4}$$

$$\frac{(x+2)^2}{1^2} + \frac{(y-3)^2}{4} = 1 \quad \text{std form}$$

Ellipse

C(-2, 3)

$$b) \quad 4x^2 - 9y^2 + 24x + 18y + 18 = 0$$

$$4x^2 + 24x - 9y^2 + 18y = -18$$

$$4(x^2 + 6x + 9) - 9(y^2 - 2y + 1) = -18 + 36 - 9$$

$$\frac{4(x+3)^2}{9} - \frac{9(y-1)^2}{9} = \frac{9}{9}$$

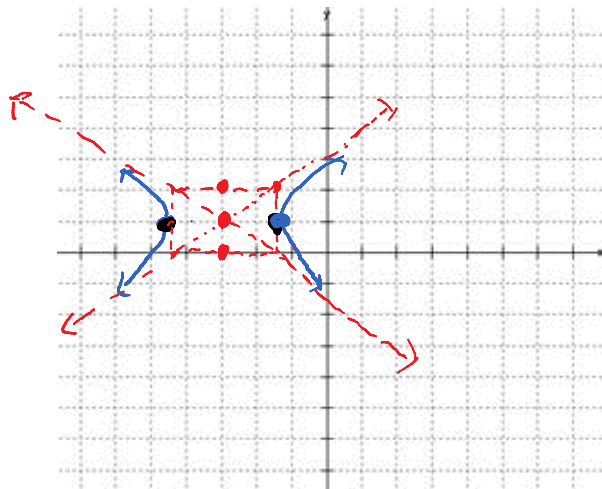
$$\frac{4(x+3)^2}{9} - (y-1)^2 = 1$$

$$\frac{(x+3)^2}{\frac{9}{4}} - \frac{(y-1)^2}{1^2} = 1$$

hyperbola

$$C(-3, 1)$$

$$\sqrt{\frac{9}{4}} = \frac{3}{2} = 1\frac{1}{2}$$



Note: $(y-1)^2 - \frac{(x+3)^2}{9/4} = 1$ graphs as ---

