

Section 9.5: Systems of Inequalities in Two Variables

Wednesday, December 03, 2014 5:23 PM

Goal: To graph the solution set of two-variable systems of inequalities.

ex) Graph the solution set to the system of inequalities

$$a) \begin{cases} 3x + 2y > 6 & \text{dotted} \\ y \leq \frac{3}{2}x - 4 & \text{solid} \end{cases}$$

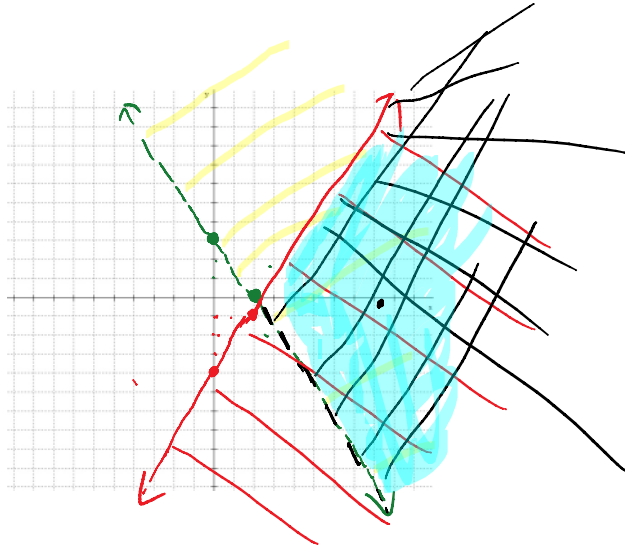
$$3x + 2y = 6$$

x	y
2	0
0	3

T.P. (0,0)

$$0 > 6 \text{ False}$$

$$y = \frac{3}{2}x - 4$$



$$b) \begin{cases} \frac{(x-4)^2}{16} - \frac{(y+2)^2}{9} > 1 & \text{dotted} \\ \frac{(x-4)^2}{36} + \frac{(y+2)^2}{9} < 1 & \end{cases}$$

hyperbola

$$\frac{(x-4)^2}{16} - \frac{(y+2)^2}{9} = 1$$

hyp. C(4,-2)

T.P. (4,-2)

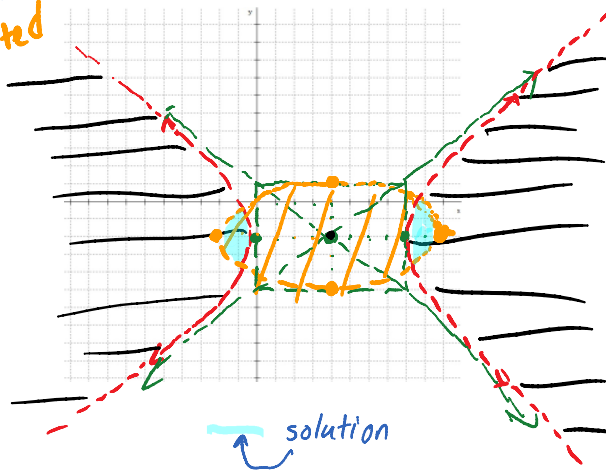
$$0 > 1$$

NO!

ellipse

$$\frac{(x-4)^2}{36} + \frac{(y+2)^2}{9} = 1$$

C(4,-2)



T.P. (4,-2)

$$0 < 1 \text{ Yes!}$$

$$c) \begin{cases} y < 2x - 1 \\ \dots \end{cases}$$

$$c) \begin{cases} y < 2x-1 \\ y \geq x^2+3x-1 \end{cases}$$

$$y = 2x - 1$$

$$(0, -1)$$

$$m = \frac{2}{1}$$

$$y = x^2 + 3x - 1$$

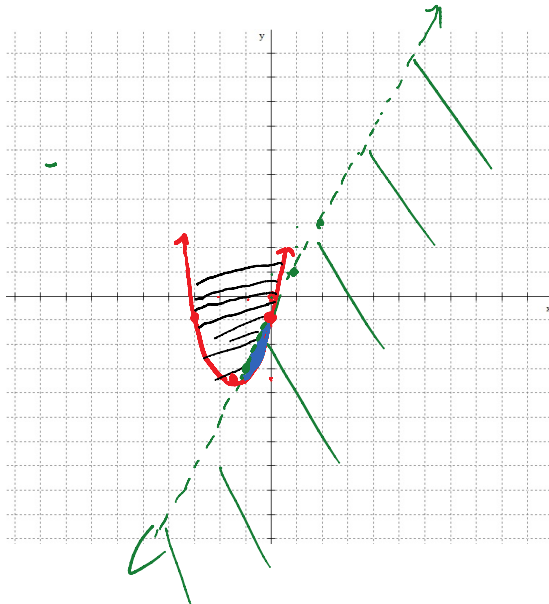
$$(h, k) = \left(\frac{-b}{2a}, f\left(\frac{-b}{2a}\right) \right)$$

$$h = \frac{-3}{2}$$

$$k = \left(\frac{-3}{2}\right)^2 + 3\left(\frac{-3}{2}\right) - 1$$

$$= \frac{9}{4} - \frac{9}{2} - \frac{1}{4}$$

$$= \frac{9}{4} - \frac{18}{4} - \frac{1}{4} = -\frac{13}{4}$$



$$V \left(\frac{-3}{2}, -\frac{13}{4} \right)$$

$$(-1.5, -3.25)$$

x	y
0	-1
-3	-1

T.P. (0, 0)

$0 \geq -1$ True!

