

Homework Section 16.2

1. Evaluate the line integral over the given curve C :

a) $\int_C 8\sqrt{x} \, ds$, $C: x = t^2, y = t, 0 \leq t \leq 2$

b) $\int_C x^4 y \, ds$, C is the upper half of the circle $x^2 + y^2 = 16$

c) $\int_C (xy + \ln y) \, dx$, C is the arc of the parabola $x = y^2$ from $(1, 1)$ to $(9, 3)$

d) $\int_C (x + y) \, dx + xy \, dy$, C consists of line segments from $(0, 0)$ to $(1, 1)$ and from $(1, 1)$ to $(2, 3)$

e) $\int_C ye^{xz} \, ds$, C is the line segment from $(0, 0, 0)$ to $(2, 1, 3)$

2. Compute the line integral $\int_C \mathbf{F} \cdot d\mathbf{r}$, where C is given by the vector function $\mathbf{r}(t)$.

a) $\mathbf{F}(x, y) = xy^2\mathbf{i} - x\sqrt{y}\mathbf{j}$, $\mathbf{r}(t) = t^3\mathbf{i} + t^2\mathbf{j}$, $0 \leq t \leq 1$

b) $\mathbf{F}(x, y, z) = \cos(x)\mathbf{i} + 2y\mathbf{j} + xz\mathbf{k}$, $\mathbf{r}(t) = t^2\mathbf{i} - t^3\mathbf{j} + 4t\mathbf{k}$, $0 \leq t \leq 1$

3. Find the work done by the force field $\mathbf{F}(x, y) = xy\mathbf{i} - y\mathbf{j}$ in moving a particle along a quarter of the unit circle from $(1, 0)$ to $(0, 1)$.

4. The figure shows a vector field \mathbf{F} and two line segments C_1 and C_2 . Determine if the respective line integrals of \mathbf{F} over C_1 and C_2 are positive, negative, or zero. Explain your answers.

