

Fun with Factoring!

Goals:

1. To factor out a Greatest Common Factor.
2. To factor by grouping.

Q: What does factoring a polynomial mean?

A: You write the poly as a product of other polys.

$$12 = (3 \cdot 4)$$

↑
a factorization
of 12

ex Factor out the greatest common factor (GCF).

$$a) \quad 6t^2 - 12t$$

$$\underbrace{6t}_{\text{GCF}} (t - 2)$$

$$6t(t - 2)$$

$$\left\{ \begin{array}{l} \text{GCF}(6, 12) = 6 \\ \text{GCF}(t^2, t) = t \\ \text{GCF}(x^6, x^4) = x^4 \end{array} \right.$$

$$b) 16t^8 + 40t^6 - 24t$$

$$8t(2t^7 + 5t^5 - 3)$$

$$c) 15m^4n + 30m^5n^2 + 25m^3n^3$$

$$5m^3n(3m + 6m^2n + 5n^2)$$

ex Factor out the negative GCF:

$$-2x^2 \cdot 1 + 4x^4 - 12x^3$$

$$-2x^2(1 - 2x^2 + 6x)$$

ex

Factor: $r(t-3) - s(t-3)$

$$(r-s)(t-3)$$

equivalent

$$(r-s)(t-3)$$

or $(t-3)(r-s)$

ex Factor by Grouping

$$a) \quad y^3 - y^2 + 3y - 3$$

$$y^2(y-1) + 3(y-1)$$

$$(y^2+3)(y-1)$$

$$b) \quad t^3 + 6t^2 - 2t - 12$$

$$t^2(t+6) - 2(t+6)$$

$$(t^2-2)(t+6)$$

$$c) \quad a^3 - 3a^2 + 6 - 2a$$

$$-2(-3+a)$$

$$a^2(a-3) - 2(a-3) \rightarrow a^3 - 3a^2 - 2a + 6$$

$$(a^2-2)(a-3)$$

↑
answer

$$d) 2y^5 + 15 - 6y^4 - 5y$$

$$2y^5 - 6y^4 - 5y + 15$$

$$2y^4(y-3) - 5(y-3)$$

$$(2y^4 - 5)(y - 3)$$

CW 5.3

① Factor out the GCF: $24x^2y^4 - 18xy^3 - 42x^4y^5$
 $6xy^3(4xy - 3 - 7x^3y^2)$

② Factor by Grouping: $xy + xz - wy - wz$
 $(y+z)(x-w)$

③ Factor by Grouping: $4x^2 + 8x + x + 2$

$$4x(x+2) + 1(x+2)$$
$$(4x+1)(x+2)$$

$$(4x+1)(x+2)$$

$$(4x+1)(x+2)$$